We discuss the Cheeger constant and some of its variants, especially in connection with Spectral Geometry in the euclidean setting. We present some results, as well as some open problems.